

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel
International GCSE**

Centre Number

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Candidate Number

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Thursday 20 June 2019

Morning (Time: 2 hours)

Paper Reference **4PM1/02**

Further Pure Mathematics

Paper 2



Calculators may be used.

Total Marks

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.
Anything you write on the formulae page will gain NO credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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Pearson

International GCSE in Further Pure Mathematics Formulae sheet

Mensuration

Surface area of sphere = $4\pi r^2$

Curved surface area of cone = $\pi r \times$ slant height

Volume of sphere = $\frac{4}{3}\pi r^3$

Series

Arithmetic series

Sum to n terms, $S_n = \frac{n}{2}[2a + (n - 1)d]$

Geometric series

Sum to n terms, $S_n = \frac{a(1 - r^n)}{(1 - r)}$

Sum to infinity, $S_\infty = \frac{a}{1 - r} \quad |r| < 1$

Binomial series

$$(1 + x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots \quad \text{for } |x| < 1, n \in \mathbb{Q}$$

Calculus

Quotient rule (differentiation)

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

Trigonometry

Cosine rule

In triangle ABC : $a^2 = b^2 + c^2 - 2bc \cos A$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A + B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A - B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A + B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A - B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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- 2 Oil is leaking from a pipe and forms a circular pool on a horizontal surface. The area of the surface of the pool is increasing at a constant rate of $8 \text{ cm}^2/\text{s}$. Find, in cm/s to 3 significant figures, the rate at which the radius of the pool is increasing when the area of the pool is 50 cm^2

(6)

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Question 2 continued

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(Total for Question 2 is 6 marks)



Question 3 continued

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(Total for Question 3 is 6 marks)



4 In triangle ABC , $AB = 5x$ cm, $BC = (3x - 1)$ cm, $AC = (2x + 5)$ cm and angle $ABC = 60^\circ$

Find, to 3 significant figures, the value of x .

(5)

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Question 4 continued

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(Total for Question 4 is 5 marks)



5 Use algebra to solve the equations

$$xy = 36$$

$$xy + x + 2y = 53$$

(6)

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Question 5 continued

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(Total for Question 5 is 6 marks)



Question 6 continued

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(Total for Question 6 is 8 marks)



Question 7 continued

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Question 7 continued

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Question 7 continued

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(Total for Question 7 is 9 marks)



Question 8 continued

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Question 8 continued

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Question 8 continued

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(Total for Question 8 is 11 marks)



Question 9 continued

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Question 9 continued

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Question 9 continued

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(Total for Question 9 is 14 marks)



Question 10 continued

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Question 10 continued

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Question 10 continued

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(Total for Question 10 is 15 marks)



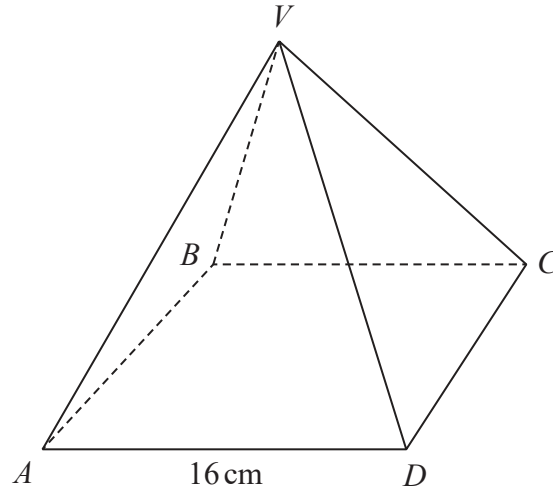


Diagram NOT accurately drawn

Figure 1

Figure 1 shows a right pyramid with vertex V and square base, $ABCD$, of side 16 cm.

The size of angle AVC is 90°

(a) Show that the height of the pyramid is $8\sqrt{2}$ cm. (4)

(b) Find, in cm, the length of VA . (3)

(c) Find, in cm, the exact length of the perpendicular from D onto VA . (3)

Find, in degrees to one decimal place, the size of

(d) the angle between the plane VAB and the base $ABCD$, (3)

(e) the obtuse angle between the plane VAB and the plane VAD . (3)

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Question 11 continued

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